

1.

a)
$$\begin{bmatrix} 235.045 \\ 128 \\ 128 \end{bmatrix}$$

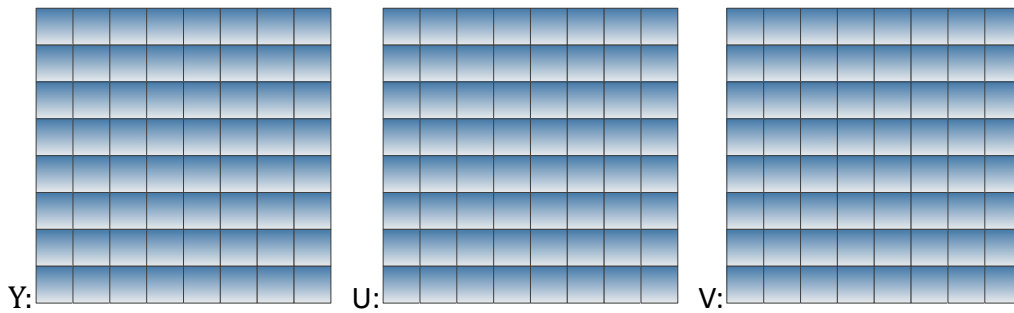
b)
$$\begin{bmatrix} 145.52 \\ 53.79 \\ 34.165 \end{bmatrix}$$

c)
$$\begin{bmatrix} 210.055 \\ 16.055 \\ 146.105 \end{bmatrix}$$

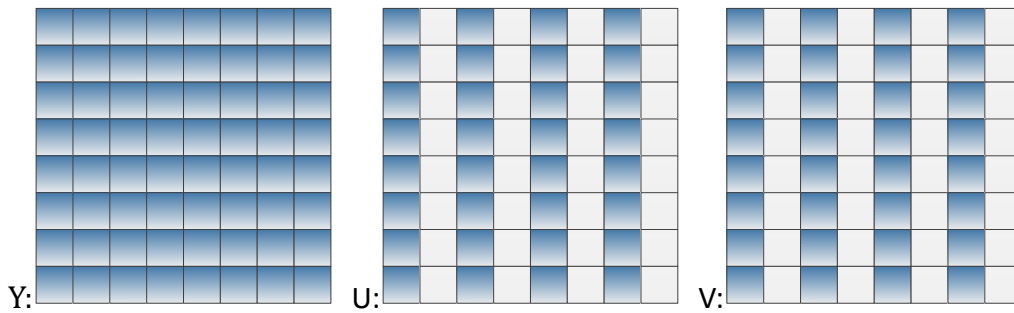
d)
$$\begin{bmatrix} 93.056 \\ 146.944 \\ 71.808 \end{bmatrix}$$

2. Use 8x8 as example for diagrams. The dark block is sampled data.

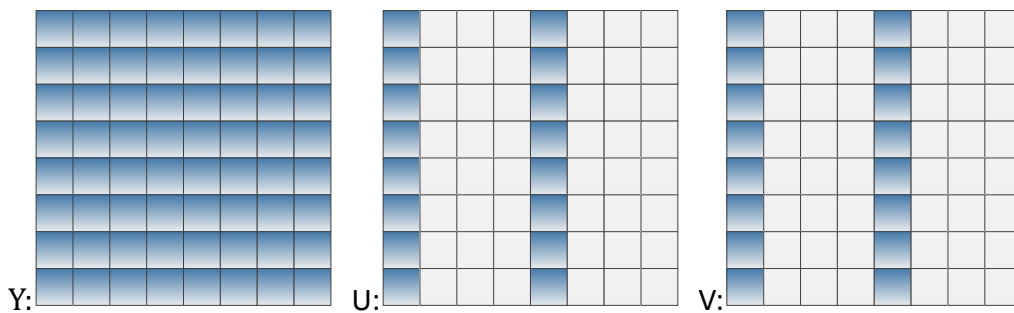
a) 4:4:4 means Y, U, V are sampled as original data.



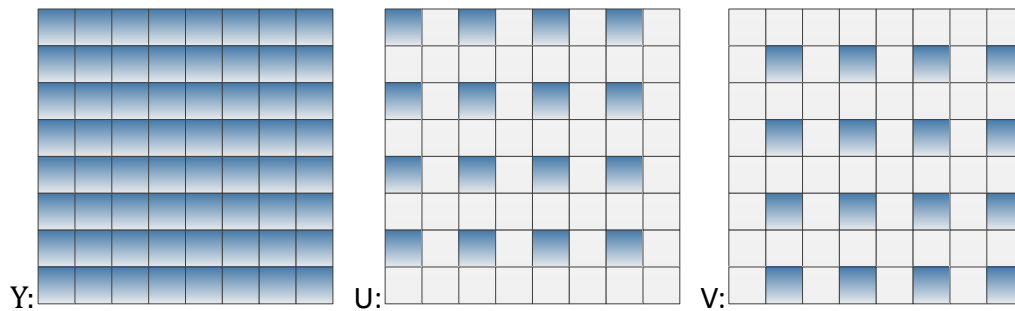
b) 4:2:2 means U, V are sampled as half of original data.



c) 4:1:1 means U, V are sampled as quarter of original data.

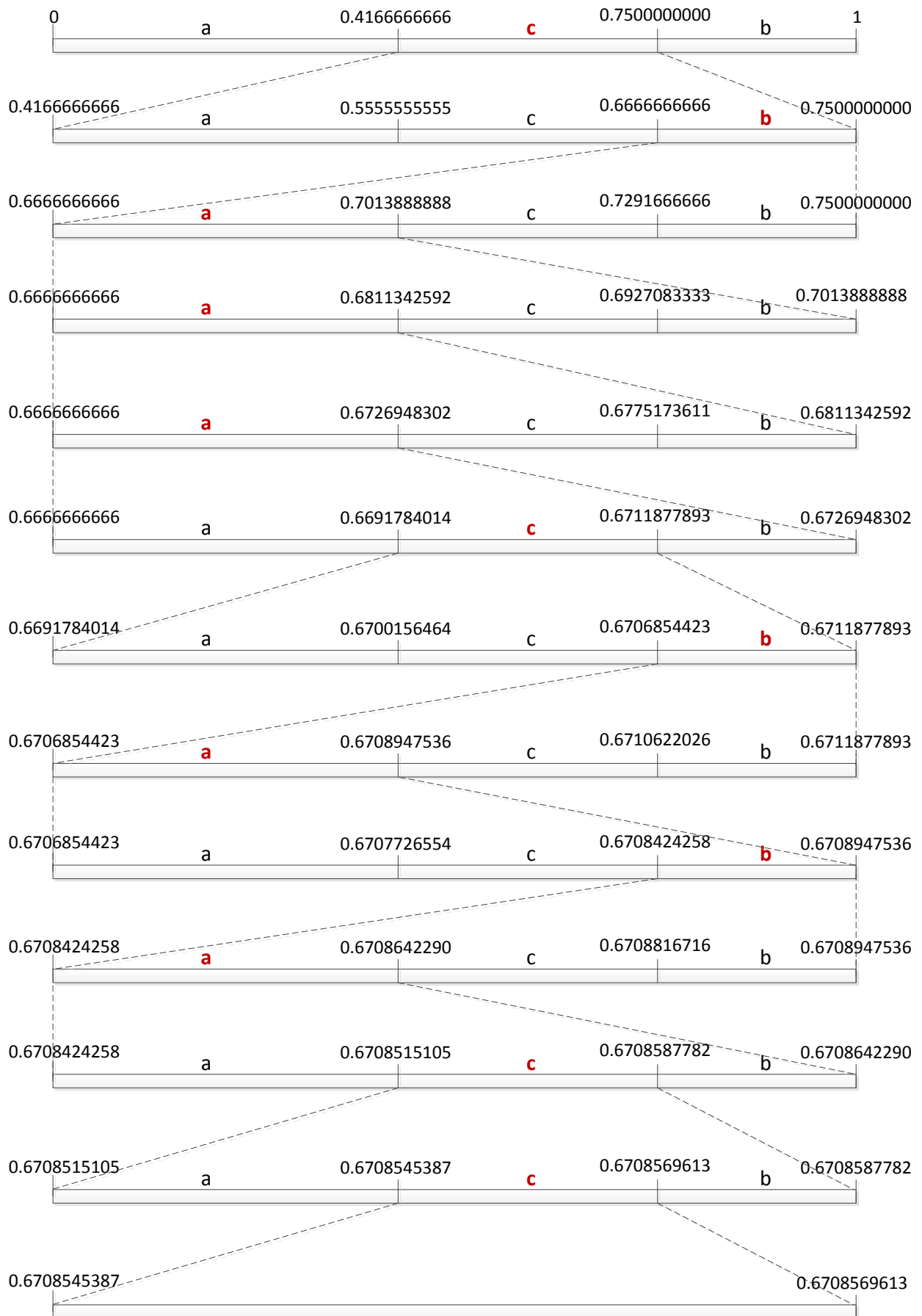


- d) 4:2:0 means U is sampled as quarter of original data for each ODD rows and V is sampled as quarter of original data for each EVEN rows.



3. **Profile** identifies subset of features to be implemented.
Level indicates encoding computation complexity.
4. Temporal scalability: Frame-rate
Spatial scalability: Resolution
SNR scalability: Quality
5. Drifting is propagating the error for future frame when intra-frame prediction is used.
Use smaller GOP size and reduce the number of B and P frame.
6. Start code is used for stream-oriented to set the boundary for each video sub-stream.
7. $H(s) = \sum_i p_i \log_2 \left(\frac{1}{p_i} \right)$
 - a) $p_i = \frac{1}{L} \Rightarrow H(s) = \sum_i \frac{1}{L} \log_2(L) \Rightarrow \log_2(L)$
 - b) $p_a = 1, p_x = 0, a \neq x \Rightarrow H(s) = p_a \log_2(1) + \sum_{a \neq x} p_x \log_2(0) \Rightarrow 0$
8. a:5, b:3, c:4 \rightarrow sort by frequency: $b = \frac{3}{12}, c = \frac{4}{12}, a = \frac{5}{12}$ and set decimal point to ten digits.
Assume each symbol encoded with two bits. Total bits is $2 \cdot 12 = 24$ bits.

Encode by Arithmetic coding:



Decode by Arithmetic coding:

Assume output value is 0.6708545387

Falls in c's interval → **output: c**

$$\frac{0.6708545387 - 0.4166666666}{\frac{4}{12}} = 0.7625636163 \text{ falls in b's interval} \rightarrow \text{output: b}$$

$$\frac{0.7625636163 - 0.7500000000}{\frac{3}{12}} = 0.0502544652 \text{ falls in a's interval} \rightarrow \text{output: a}$$

$$\frac{0.0502544652 - 0.0000000000}{\frac{5}{12}} = 0.1206107164 \text{ falls in a's interval} \rightarrow \text{output: a}$$

$$\frac{0.1206107164 - 0.0000000000}{\frac{5}{12}} = 0.2894657193 \text{ falls in a's interval} \rightarrow \text{output: a}$$

$$\frac{0.2894657193 - 0.0000000000}{\frac{5}{12}} = 0.6947177263 \text{ falls in c's interval} \rightarrow \text{output: c}$$

$$\frac{0.6947177263 - 0.4166666666}{\frac{4}{12}} = 0.8341531791 \text{ falls in b's interval} \rightarrow \text{output: b}$$

$$\frac{0.8341531791 - 0.7500000000}{\frac{3}{12}} = 0.3366127164 \text{ falls in a's interval} \rightarrow \text{output: a}$$

$$\frac{0.3366127164 - 0.0000000000}{\frac{5}{12}} = 0.8078705193 \text{ falls in b's interval} \rightarrow \text{output: b}$$

$$\frac{0.8078705193 - 0.7500000000}{\frac{3}{12}} = 0.2314820772 \text{ falls in a's interval} \rightarrow \text{output: a}$$

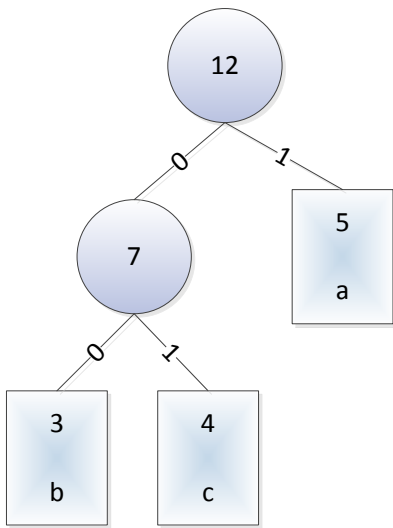
$$\frac{0.2314820772 - 0.0000000000}{\frac{5}{12}} = 0.5555569852 \text{ falls in c's interval} \rightarrow \text{output: c}$$

$$\frac{0.5555569852 - 0.4166666666}{\frac{4}{12}} = 0.4166709558 \text{ falls in c's interval} \rightarrow \text{output: c}$$

$$\frac{0.4166709558 - 0.4166666666}{\frac{4}{12}} \approx 0, \text{ Done}$$

Output: **c, b, a, a, a, c, b, a, b, a, c, c**

Encode by Huffman coding:



a: 1

b: 00

c: 01

cbaaacbabacc → 0100111010010010101 (Total 19 Bits)