

Moving object detection, tracking and following using an omnidirectional camera on a mobile robot

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Outline

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Introduction

- **Omnidirectional cameras** are powerful in **mobile robot's vision system**, due to it stored all information about the surrounding scene
- **Panoramic videos** provide more information than conventional video, it increase the robot's abilities to react in the environment
- Combine omnidirectional cameras and mobile robot, for example, removing the possibility that the followed object will escape the camera's field-of-view
- However, detecting, tracking, and following the moving object with a camera mounted on a mobile robot is challenging
- Because of **the motion of the simultaneous** ego-motion of the robot and the motion of the object

Camera calibration

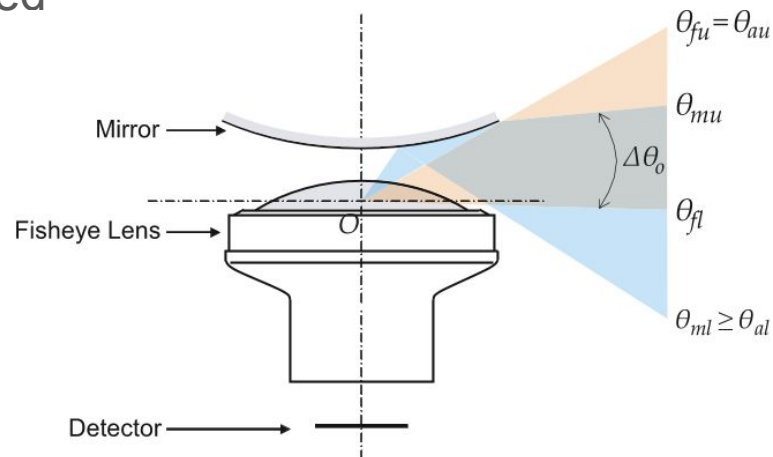
- An omnidirectional camera, which contains a fisheye lens (a wide-angle lens) with a catadioptric lens (a mirror) called catadioptric system [1]
- It mounted on a mobile robot to obtain the panoramic image
- **Pros:** decrease the stitching issues at the edges of the projection
- **Cons:** a unique calibration method is needed



(c)



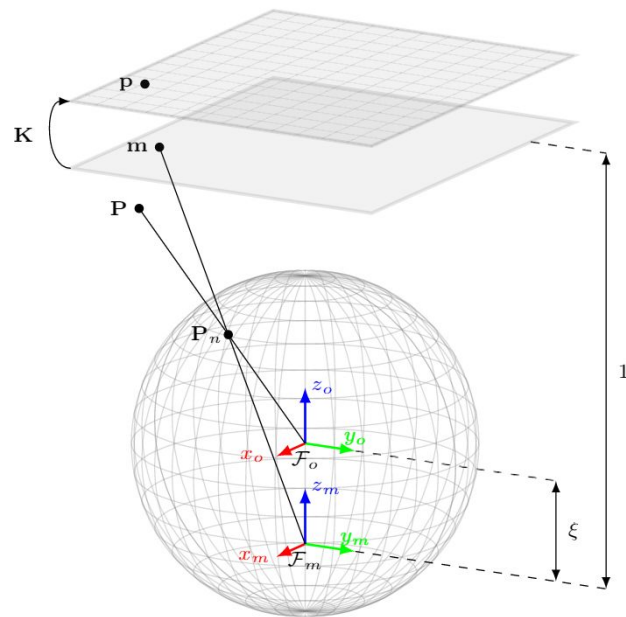
(d)



Camera calibration (cont.)

- Single view point omnidirectional camera calibration from planar grids
- K is a 3x3 matrix containing the camera intrinsic parameters
- K and ξ are obtained by the calibration procedure
- **planar -> sphere**

$$\mathbf{m} = \mathbf{K}^{-1}\mathbf{p}, \quad \mathbf{P}_n = \begin{bmatrix} \frac{\xi + \sqrt{1 + (1 - \xi^2)(x^2 + y^2)}}{x^2 + y^2 + 1} x \\ \frac{\xi + \sqrt{1 + (1 - \xi^2)(x^2 + y^2)}}{x^2 + y^2 + 1} y \\ \frac{\xi + \sqrt{1 + (1 - \xi^2)(x^2 + y^2)}}{x^2 + y^2 + 1} - \xi \end{bmatrix}. \quad (1)$$



[2] https://en.wikipedia.org/wiki/Lucas%E2%80%93Kanade_method

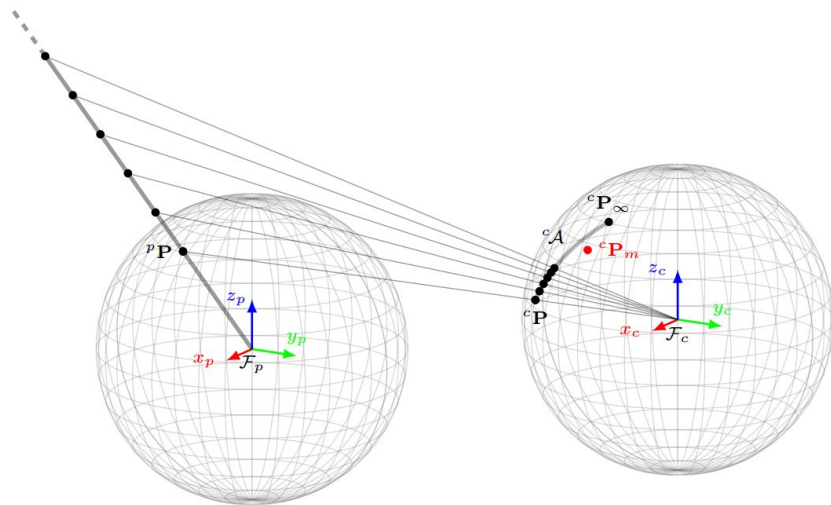
[3] <http://ieeexplore.ieee.org/document/6046621/>

Object detection

- Detect moving object in the omnidirectional image while the robot itself moves
- Motion in the image **is caused by moving object and ego-motion of robot**
- To figure out this challenge, they calculate the **sparse optical flow** (Lucas-Kanade algorithm [2]) in the image, which caused by the ego-motion and moving object [3]
- Sparse techniques only process some pixels from the whole image

Object detection (cont.)

- Now, we need to find the optical flow caused by the moving object only
- \mathcal{F}_p : previous frame
- \mathcal{F}_c : current frame
- ${}^c\mathbf{R}_p$: rotation
- ${}^c\mathbf{t}_p$: translation
- ${}^p\mathbf{P}$: point in previous frame
- ${}^c\mathbf{P}_m$: point in current frame



- First, hypothesize the flow was ego-motion, if the condition is not met, it should be caused by the moving object

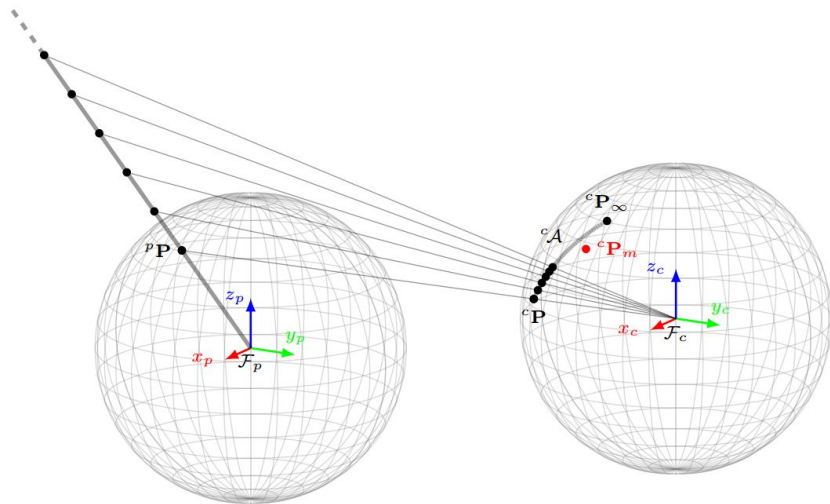
Object detection (cont.)

- ${}^c\mathbf{P}_\infty = {}^c\mathbf{R}_p {}^p\mathbf{P}$
- ${}^p\mathbf{P}$ represent a point on the previous sphere
- If an optical flow as caused by ego-motion if its matched point on the current sphere ${}^c\mathbf{P}_m$ lies somewhere along the arc of the great circle
- Great circle distance

$$d({}^c\mathbf{P}, {}^c\mathbf{P}_\infty) = \arccos({}^c\mathbf{P} \cdot {}^c\mathbf{P}_\infty), \quad (2)$$

- Calculate the distance of ${}^c\mathbf{P}_m$ to arc ${}^c\mathcal{A}$

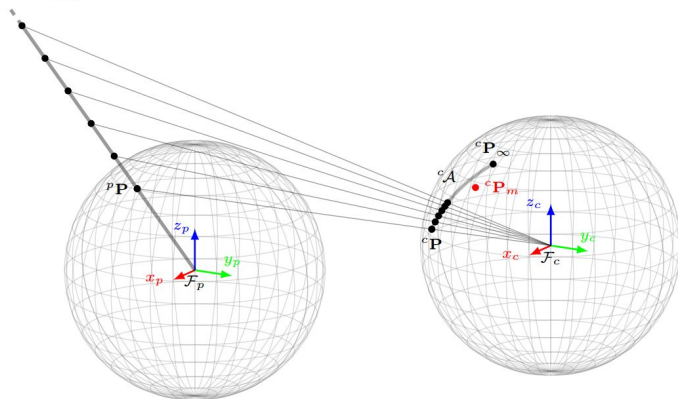
$$\mathbf{P}' = {}^c\mathbf{P}_m - ({}^c\mathbf{P}_m \cdot \mathbf{n}) \mathbf{n}, \quad {}^c\mathbf{Q}_m = \frac{\mathbf{P}'}{|\mathbf{P}'|}, \quad (3)$$



Object detection (cont.)

- If ${}^c\mathbf{Q}_m$ lies on ${}^c\mathcal{A}$ the distance of the point ${}^c\mathbf{P}_m$ to the arc ${}^c\mathcal{A}$ is calculated as $d({}^c\mathbf{P}_m, {}^c\mathbf{Q}_m)$
- If not, $\min\{d({}^c\mathbf{P}_m, {}^c\mathbf{P}), d({}^c\mathbf{P}_m, {}^c\mathbf{P}_\infty)\}$
- If the robot does not move or just rotate, then (4) is false, otherwise is true

$$\begin{aligned}
 &({}^c\mathbf{P} \times {}^c\mathbf{Q}_m) \cdot ({}^c\mathbf{Q}_m \times {}^c\mathbf{P}_\infty) > 0 \quad \text{and} \\
 &({}^c\mathbf{P} \times {}^c\mathbf{Q}_m) \cdot ({}^c\mathbf{P} \times {}^c\mathbf{P}_\infty) > 0.
 \end{aligned}
 \tag{4}$$



[4] https://en.wikipedia.org/wiki/Bayes%27_theorem

[5] https://en.wikipedia.org/wiki/Von_Mises%E2%80%93Fisher_distribution

Object tracking on the sphere

- To pose a probabilistic model of the sensor measurement, they using **Bayesian estimation [4] tracker** based on the **von Mises-Fisher distribution [5]**
- The distribution has the following form, μ is the mean direction and κ is the concentration parameter

$$p(\mathbf{x}; \kappa, \boldsymbol{\mu}) = \frac{\kappa}{4\pi \sinh \kappa} \exp(\kappa \boldsymbol{\mu}^T \mathbf{x}), \quad (5)$$

- The larger the κ , the greater the clustering around the mean direction

Object tracking on the sphere (cont.)

- Two steps: (1)prediction and (2) update
- In prediction, the probability density function (pdf) is:

$$p(\mathbf{x}_k | \mathbf{z}_{1:k-1}) = \int p(\mathbf{x}_k | \mathbf{x}_{k-1})p(\mathbf{x}_{k-1} | \mathbf{z}_{1:k-1}) d\mathbf{x}_{k-1}, \quad (6)$$

- In update, the result of update step is a VMF with the following parameters

$$\kappa_{ij} = A^{-1}(A(\kappa_i)A(\kappa_j)), \quad A(\kappa) = \frac{1}{\tanh \kappa} - \frac{1}{\kappa}. \quad (7)$$

$$\kappa_{ij} = \sqrt{\kappa_i^2 + \kappa_j^2 + 2\kappa_i\kappa_j(\boldsymbol{\mu}_i \cdot \boldsymbol{\mu}_j)}, \quad \boldsymbol{\mu}_{ij} = \frac{\kappa_i\boldsymbol{\mu}_i + \kappa_j\boldsymbol{\mu}_j}{\kappa_{ij}}. \quad (9)$$

- This will produce the estimate of the direction of the moving object
- They only track a single object, if there are multiple objects, it will track the **closest measurement** one in the update step

Object following

- To follow the tracked moving object, they propose to use visual servoing technique to solve this problem
- **Visual servoing [6]**: a technique which uses feedback information from a vision sensor to control the motion of a robot
- They use cylindrical coordinate system, so the direction \mathbf{x}_k on the sphere is:

$$\rho = \sqrt{s_x^2 + s_y^2}, \quad \theta = \arctan \frac{s_y}{s_x}. \quad (10)$$

- **Control law** based on (1) linear velocity v and (2) angular velocity w

$$\mathbf{v} = (v, \omega)$$

- Spatial velocity is $\dot{\mathbf{s}} = \mathbf{L}_s \mathbf{v}$

Object following (cont.)

- The interaction matrix is

$$\mathbf{L}_s = \begin{bmatrix} \frac{-\cos \theta}{P_z} & 0 \\ \frac{\sin \theta}{\rho P_z} & -1 \end{bmatrix}, \quad (11)$$

- Control law is

$$\begin{bmatrix} v \\ \omega \end{bmatrix} = -\lambda \hat{\mathbf{L}}_s^{-1} \begin{bmatrix} \rho - \rho^* \\ \theta - \theta^* \end{bmatrix}, \quad (12) \quad \dot{\mathbf{s}} = \mathbf{L}_s \mathbf{v}$$

- e is the **error** (great circle distance) of the control task

$$\lambda(e) = a \exp(-be) + c, \quad (13) \quad \begin{aligned} a &= \lambda(0) - \lambda(\infty), b = \lambda'(0)/a, c = \lambda(\infty) \\ \lambda(0) &= 0.5, \lambda(\infty) = 0.05, \lambda'(0) = 0.5 \end{aligned}$$

Experiment results

- Object moved so as to first distance itself from the desired position and then waited until the robot closed the distance **by reducing the servoing task error to zero** ([demo](#))

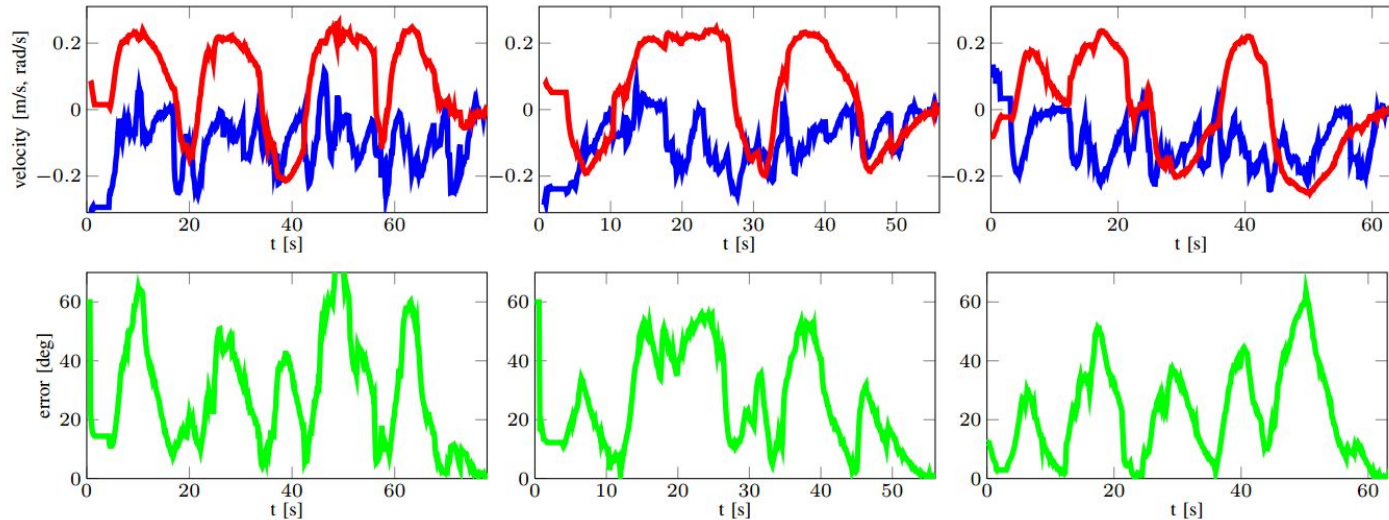


Fig. 5. Command velocities—linear (red) and angular (blue), and error of the control task (great circle distance from the desired to the estimated direction)

Conclusion

- They use an omnidirectional camera, which contains a fisheye lens (a wide-angle lens) with a catadioptric lens (a mirror), mounted on a mobile robot to obtain the panoramic image
- The amount of information in a panoramic image **increase the robot's abilities in reacting in the environment**
- They present a method based on sphere for detecting moving object, tracking, and following it

Q & A